EFFECT OF SLABS IN SPACE FRAMED STRUCTURES UNDER SEISMIC LOADING

F.K Abdel Sayed 1, Ahmed. Abdel Reheem Farghly 2, Shehata. E. Abdel Reheem 3, Ashraf A. Mohamed 4 and M. N. Mohamed 5, *

1, 3, 4 Staff in Civil Eng. Dep., Faculty of Engineering, Assiut University, Assiut, Egypt
2 Civil and Architectural Constructions Department Industrial Education College, Sohag University, Sohag, Egypt
5 Technical Marketing Manager, CEMEX Company

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Abstract

Frame system structures which composed of only reinforced concrete columns, beams and slabs, have been widely adopted for many framed buildings. Generally, in-plane stiffness of slabs is ignored in the conventional analysis of such structures. However, in reality, the floor slabs may have some influence on the lateral response of the structures. Consequently, if the in-plane stiffness of slabs in a frame system structure is totally ignored, the lateral stiffness of the global frames may be underestimated. Therefore, the objective of the research is to investigate the effect of floor diaphragms in multi-story frames by comparing frames models with different slabs thickness by those without slabs. Furthermore, it can be seen from the study that the slab thickness is an important factor increasing in-plane stiffness of the slab and consequently increasing the overall in-plan stiffness of the building leading to an increase in base shear and a decrease in lateral displacements values.

Keywords: rigid floor diaphragm, flexible floor diaphragms, in-plan deformation, floor diaphragm action and time history analysis

1. Introduction

Floor diaphragms in-plane stiffness affects building response to seismic ground accelerations; it is generally provided primarily to resist out-of-plane vertical gravity loads in the structure. However, for reliable performance, there diaphragms must resist lateral forces (such as earthquake) and transfer them dependably to the vertical lateral force resisting elements (such as walls and frames) within a structure [7].

Under Seismic loading, floor systems in reinforced concrete (RC) buildings act as diaphragm to transferee lateral earthquake loads to the vertical lateral force-resisting system [3].

Floor in-plane stiffness plays an important role in distributing seismic forces to lateral-resisting elements. In most cases, the assumption of rigid floor allows a significant reduction of computational effort in the structural analysis of buildings. In some cases, however, structural configurations with large spans between lateral resisting elements can invalidate the use of the rigid-floor assumption. For these cases, diaphragm flexibility must be considered in the analysis. Moreover, in the case of plans with irregular distributions of mass or stiffness, torsional unbalance can exacerbate the effects of floor flexibility [2]. Additionally, when the structure stiffness increases it can absorb greater lateral forces induced by the earthquake motions [8].

* Corresponding author.
E-mail address: mnace2003@hotmail.com
To study the effect of diaphragm action of floor slabs on building response, first, this paper discusses in-plan characteristics of R.C. floor slabs, the most critical factor to control the diaphragm action, on the basis of the results of previously conducted experiments [4], [5].

So, in order to predict accurate lateral displacements and base shear values of a frame system structures, it may be prudent to include in-plane stiffness of slabs.

“The problem statement of this research is to find out the relationship between lateral stiffness and both base shear values and lateral deflection of frames based on in-plane stiffness of slabs”.

2. Aims and Objectives

Numerical methods have been widely used in solving engineering non-linear problems. Therefore, the main objectives of this study are:

- To monitor and analyze the effect and the contribution of the below parameters on both base shear values and lateral displacements of high-rise building under seismic loading:
  1. The effect of slabs (slab thickness or diaphragm effect).
  2. Rectangularity ratio of the building plan.

3. Model Description

The study will conduct non-linear finite element analysis using SAP2000 program for the frame.

Figure 1 shows the structural plan of the used model, a 30 story building, with identical plan (as shown in figure 1) have been considered in the analysis. The overall plan dimensions are 6.0m x 6.0m for each bay (2x2 bay, 2x4 bays and 2x6 bays with three corresponding rectangularity ratios, length / width ratio = 1: - 1:2 – 1:3 respectively), measured from the centre line of the columns. The height of the ground floor is 3.0m and inters stories heights are 3m. The thickness of the analyzed slab models has been considered as: no existing slabs, 8cm, 10cm and 12cm. Columns are with size at ground and first floors with 70x70 cm dimension and 24ø16mm, and dimensions of columns reduced by 5cm in both directions every 2 floors until reaching columns size 40x40cm, 6ø8/m’ stirrups reinforcement, and beams with constant size 25x50cm and 4ø16mm bottom and upper reinforcement, 7ø8mm/m’ stirrups reinforcement.

3.1. Input loadings

A time history analysis was carried out using El Centro earthquake which has maximum acceleration 0.5g (figure 2) the earthquake affects on Y directions of the tested model.
4. Results and Discussion

Three models were undertaken, three different rectangularity ratios (length / width ratio = 1: - 1:2 – 1:3) to discuss the effects of slab diaphragm on the 3D frame seismic analysis. The effects of slabs thickness or absence was measured by the values of displacement of some selected points (point (1) and point (2) as shown in figure 1) and compare its displacements values in direction perpendicular on the length of the tested models to show after that the effects of slab diaphragm on base shear.

First: Study the effect on lateral displacements values:
In this part, in purpose to show the in-plan deformation and the effect of diaphragm on the lateral distortion of the floor plan, three main analyzed cases will be discussed as follows:
The first case

Figures (3-i, 3-ii, 3-iii and 3-iv) represent the displacements in y direction for the selected points (1), (2) in case of 30 story building, 2x6 bay (rectangularity ratio = 1:3 as shown in figure 1-i) and various slab cases (No slab, 8cm, 10cm and 12cm).

Figure (3-i) shows the comparison between displacement in y direction for points (1) and (2) in case of no slab, at floors (from 9 to 30 stories) there is a clear difference between the two selected points in average 21.7% against 5.5% in the first nine floors, this means that these points are deformed each one alone. Figure (3-ii) using 8cm slab (diaphragm) shows a less diversion between the two values of displacements in y direction for all floors except a slightly difference between the two points displacements in the last floors in average = 1.4%. And for figure (3-iii) using a 10cm slab less diversion occurred, while in figure (3-iv) with using 12cm slab thickness, the difference between lateral displacement (Uy) of points (2) and (1) = zero all over the building (rigid floor diaphragm effect).

- So it can be stated that:
  1. By increasing slab thickness the difference between points (1) and (2) displacements are reduced, reaching zero in high stiffness slab such as in case of 12cm. (means that by increasing slab thickness, the slab acts as a rigid diaphragm).
  2. Increasing slab thickness (stiffness) reduces the average lateral displacements values. This inverse relation is demonstrated in the below two examples:
    2-1 The average displacements were 24.7, 17.41, 16.8 & 15.1 in the four scenarios of slabs thickness (no slab, 8, 10, 12cm) respectively.
    2-2 By monitoring the reduction in displacements of each point (1) and (2) separately, when increasing slab thickness from zero thickness (no slab) to 12cm, the below reductions percentages in the point’s displacements were occurred:
      o 31% for point (1) and 35.6% for point (2) in the first floor.
      o 24.9% for point (1) and 41.3% for point (2) in the last floor.
  3. The maximum displacement occurred in the four cases in the last floor while the minimum displacement occurred in the first floor, it was also noticed in no slab case that after the eighth floor approximately the diversion started to be more significant and the higher story have bigger difference between the displacements of the two points (1,2).

Fig 3. i. Comparison between lateral displacements of points (1) and (2) in 30 story building, 2x6 bay and no slab model

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Fig. 3. **ii.** Comparison between lateral displacements of points (1) and (2) in 30 story building, 2x6 bay, 8cm slab model

Fig. 3. **iii.** Comparison between lateral displacements of points (1) and (2) in 30 story building, 2x6 bay, 10cm slab model

Fig. 3. **iv.** Comparison between lateral displacements of points (1) and (2) in 30 story building, 2x6 bay, 12cm slab model
The second case

Figures (4-i, 4-ii, 4-iii and 4-iv) represent the displacements in y direction for the selected points (1), (2) in case of 30 story building, 2x4 bay (rectangularity ratio = 1:2 as shown in figure 1-ii) and various slab cases (No slab, 8cm, 10cm and 12cm). Figure (4-i) shows the comparison between displacement in y direction for points (1) and (2) in case of no slab, there are clear differences between the two selected points in average equal 11.7%, this means that these points in general are deformed each one alone. On the other hand from figures (4-ii), (4-iii) and (4-iv) using 8cm,10cm & 12cm slab (diaphragm) respectively, it is so clear that the difference between lateral displacement (Uy) of points (2) and (1) equal zero all over the building, (means that, the slab worked as a rigid diaphragm).

• So it can be stated that:
  1. By increasing slab thickness the difference between points (1) and (2) displacements are reduced, reaching zero in high stiffness slab (as in slabs thickness 8, 10 and 12 cm cases), means that by increasing slab thickness, the slab acts as a rigid diaphragm.
  2. Increasing slab thickness (stiffness) reduces the average lateral displacements values. This inverse relation is demonstrated in the below two examples:
    2-1 The average displacements were 18.6, 14.7, 13.3 & 12 in the four scenarios of no slab, 8, 10, 12 cm slab thickness respectively (means that by increasing slab thickness the displacements were reduced).
    2-2 By monitoring the reduction in displacements of each point (1) and (2) separately, when increasing slab thickness from zero thickness (no slab) to 12cm, the below reductions percentages in the point’s displacements were occurred:
      ▪ 7.5% for point (1) and 21.3 % for point (2) in the first floor
      ▪ 33% for point (1) and 39% for point (2) in the last floor
  3. The maximum displacement occurred in the four cases in the last floor while the minimum displacement occurred in the first floor, it was also noticed in no slab case that the higher story have bigger difference between the displacements of the two points (1,2).

![Fig. 4. i. Comparison between lateral displacements of points (1) and (2) in 30 story building, 2x4 bay and no slab model](image)
**Fig. 4. ii.** Comparison between lateral displacements of points (1) and (2) in 30 story building, 2x4 bay, 8cm slab model

**Fig. 4. iii.** Comparison between lateral displacements of points (1) and (2) in 30 story building, 2x4 bay, 10cm slab model

**Fig. 4. iv.** Comparison between lateral displacements of points (1) and (2) in 30 story building, 2x4 bay, 10cm slab model
The Third Case

Figures (5-i, 5-ii, 5-iii and 5-iv) represent the displacements in y direction for the selected points (1), (2) in case of 30 story building, 2x2 bay (rectangularity ratio = 1:1 as shown in figure 1-ii) and various slab cases (No slab, 8cm, 10cm and 12cm).

From figures (5-i, 5-ii, 5-iii and 5-iv) it can be observed that, although the reduction of maximum displacement by increasing slab thickness, there are a difference between the lateral displacements in all cases between the two points. Also it is the only case between the three cases that point (1) displacements values are more than point (2)

- So it can be stated that:
  1. By increasing slab thickness the difference between points (1) and (2) displacements are reduced, (Average differences = 40/% in case of no slab, and equal = 38.5% in the three other cases when slab thickness = 8cm, 10cm, 12cm) (flexible floor diaphragms effect).
  2. There is inverse relationship between slab thickness and points lateral displacements .for example:
     2-1 The average displacements were 16.7, 14.6, 13.0 & 12.1 in the four scenarios of no slab, 8, 10, 12 cm slab thickness respectively.
     2-2 By monitoring the reduction in displacements of each point (1) and (2) separately, when increasing slab thickness from zero thickness (no slab) to 12cm, the below reductions percentages in the point’s displacements were occurred:
       o In the first floor, by 26.2% for point (1) and 17.6% for point (2).
       o In the last floor, by 26.3% for point (1) and 26.1% for point (2).
  3. The maximum displacement occurred in the four cases in the last floor while the minimum displacement occurred in the first floor, it was also noticed in no slab case that the higher story have bigger difference between the displacements of the two points (1,2).

![Fig. 5. i. Comparison between lateral displacements of points (1) and (2) in 30 story building, 2x2 bay and no slab model](image)

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Fig. 5. **ii.** Comparison between lateral displacements of points (1) and (2) in 30 story building, 2x2 bay, 8cm slab model

Fig. 5. **iii.** Comparison between lateral displacements of points (1) and (2) in 30 story building, 2x2 bay, 10cm slab model

Fig. 5. **iv.** Comparison between lateral displacements of points (1) and (2) in 30 story building, 2x2 bay, 12cm slab model
The effect of rectangularity ratio on lateral displacements values:

From the above three cases, the below findings were observed:

- When comparing the effect of the slab thickness (diaphragm effect) in the three rectangularity ratio cases (1:1, 1:2, 1:3), it can be stated that, slab thickness has a strong influence on reducing the average lateral displacements and this influence are increased by increasing rectangularity ratio, as illustrated by the below example and shown in table (1):
  - In the first case: when rectangularity ratio = 1:3, increasing slab thickness from no slab scenario to 12cm thickness leads to decrease the average lateral displacements by 38.9%
  - In the second case: when rectangularity ratio = 1:2, increasing slab thickness from no slab scenario to 12cm thickness leads to decrease the average lateral displacements by 34.9%
  - In the third case: when rectangularity ratio = 1:1, increasing slab thickness from no slab scenario to 12cm thickness leads to decrease the average lateral displacements by 28.1%

From the above it is clear that by increasing the rectangularity ratio the reduction occurred to the lateral displacement when increasing slab thickness become more significant.

Table 1.

indicates the average displacements (cm) of the two point (1,2) for 30 story building

<table>
<thead>
<tr>
<th>Average displacements (cm)</th>
<th>Rectangularity Ratio</th>
<th>No slab case</th>
<th>Slab thickness (cm)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td>8cm</td>
</tr>
<tr>
<td>1:3 (2x6 bay)</td>
<td>24.7</td>
<td>17.4</td>
<td>16.8</td>
</tr>
<tr>
<td>1:2 (2x4 bay)</td>
<td>18.6</td>
<td>14.7</td>
<td>13.3</td>
</tr>
<tr>
<td>1:1 (2x2 bay)</td>
<td>16.7</td>
<td>14.6</td>
<td>13</td>
</tr>
</tbody>
</table>

It is worthy to mention that in no slab case, the lateral displacements of point (1) are less than the lateral displacements of point (2), this is occurred in two cases of rectangularity ratio (1:3 and 1:2), while in case of rectangularity ratio 1:1 the lateral displacements of point (1) are more than the lateral displacements of point (2).

Second: Study the effect on base shear values:

Figure 6 indicates the differences between the values of base shear for the three models with fixed stories no = 30 story and different rectangularity ratio (1:1, 1:2 and 1:3) with various slab thickness.

From figure 6, the below relationships can be estimated:

1 – There is direct relationship between base shear value and slab thickness, this relationship is indicated in the below percentages:

- In case of rectangularity ratio = 1:3, the increasing percentage in base shear value = 211% when increasing slab thickness from no slab case to 12 cm thickness.
- In case of rectangularity ratio = 1:2, the increasing percentage in base shear value = 317% when increasing slab thickness from no slab case to 12 cm thickness.
- In case of rectangularity ratio = 1:1, the increasing percentage in base shear value = 375% when increasing slab thickness from no slab case to 12 cm thickness.
From the above percentages, it is obviously obtained that when increasing slab thickness and decreasing the rectangularity ratio the influence of slabs thickness in increasing base shear value become more effective and clear.

2. There is direct relationship between base shear value and rectangularity ratio.
   - The base shear value increased in average by 54% when increasing rectangularity ratio from 1:1 (2x2 bays) to 1:2 (2x4) case.
   - The base shear value increased in average by 27% when increasing rectangularity ratio from 1:2 (2x4 bays) to 1:3 (2x6) case.

![Comparison between base shear values in 30 story building with various rectangularity ratios 1:1, 1:2 and 1:3 (2x2, 2x4 and 2x6 bays) models with different slab thickness](image)

Fig. 6. Comparison between base shear values in 30 story building with various rectangularity ratios 1:1, 1:2 and 1:3 (2x2, 2x4 and 2x6 bays) models with different slab thickness

4. Conclusions

According to the results obtained from the studied cases it can be stated that slab in-plane stiffness (Diaphragm) has significant influence in the response of high-rise building under seismic loading, this influence can be concluded as follows:

1. **Influence on the lateral displacements:**
   - Increasing slab thickness under seismic loading, works on reducing the overall average lateral displacements of the building.
   - Additionally, the thickness of the slab (diaphragm effect) has a strong influence on reducing the differential lateral displacements hence avoiding as possible any probable distortion.
   And so, it can be concluded that, in this study there is an inverse relationship between slab in-plane stiffness (thicknesses) with both lateral displacements and differential lateral displacements.
   - Slab in-plan stiffness has a clear influence on reducing the average lateral displacements and this influence increases by increasing rectangularity ratio as follows:
     - The average decreasing percentage that occurred to lateral displacements due to increasing slab thickness from zero slab to 8cm to 10cm to 12cm, for the three rectangularity ratios 1:1, 1:2 and 1:3 are 31.2%, 39.5% and 43.1% respectively.
Increasing rectangularity ratio leads to increase lateral displacements values. The corresponding average displacements values for 30 story building with slab thickness = 10cm were 16.8, 13.3 and 13.0 cm for rectangularity ratios = 1:3, 1:2 and 1:1 respectively.

There is direct relationship between number of stories and both lateral displacements values and the differential lateral displacements.

2. **Influence on the base shear values:**

Also the present study introduced an analysis concerning the effect of slab thickness (lateral stiffness) and rectangularity ratio on the value of base shear under seismic loading, and from this study the below relationships can be stated as follows:

- There is direct relationship between base shear value and slab thickness, in addition to that it is obviously obtained that when increasing slab thickness and decreasing the rectangularity ratio the influence in increasing base shear value become more significant as follows:
  - By increasing slab thickness from zero slab case to 12 cm thickness in 30 story building the percentage increasing in base shear values were: 211%, 315% and 375% for rectangularity ratios 1:3, 1:2 and 1:1 respectively.

- There is direct relationship between base shear value and rectangularity ratio. The base shear value increased in average by 40.5% when increasing rectangularity ratio in the two following cases: from 1:1 (2x2 bays) to 1:2 (2x4 bay) and from 1:2 (2x4 bays) to 1:3 (2x6 bay).

Finally, based on the above results, this research proved that the slab in-plane stiffness (floor diaphragm action) plays clear and important role in decreasing the overall lateral displacement of the high-rise building under seismic loading, also it works on reducing differential lateral displacements. Furthermore increasing building rectangularity leads to increasing the effectiveness of slabs for decreasing lateral displacements values.

- Also through the presented study, it was proved that there are direct relationships between base shear value and both of slab thickness and rectangularity ratio.

- So, it can be seen from the study that the slab actually is acting important role to increase the overall in-plan stiffness of the models leading to increase the base shear and reduce both lateral displacements and in-plan deformation (lateral distortion). However, the Egyptian code (201/2008) neglects the effect of slab in-plane stiffness (thickness) in calculating both base shear values and lateral displacements, leading to high displacements values and low base shear far from the actual behavior resulting in an inaccurate design.

Therefore, this study strongly recommends that such important parameter, Diaphragm effect (slab thickness) should be taken into account in computing base shear value and lateral displacements in multi-story building under seismic loading.

5. **References**

تأثير البلاطات في منشآت الأطر الفراغية تحت تأثير الحمل الزلزالي

الملخص العربي

تهدف هذه الدراسة للتحقق من تأثير سمة البلاطة (الدابيرام) على السلوك الإنشائي للمباني عالية الارتفاع الواقعة تحت تأثير الحمل الزلزالي.

دراسة تأثير البلاطات (الدابيرام) تحت تأثير الحمل الزلزالي على منشآت الأطر الفراغية عالية الارتفاع تم عمل التحليل الإنشائي لعدد 30 منشأة (نمادج) ذات ارتفاع ثابت 3 م وبحث استطالة مختلفة (نسبة الطول / الارتفاع) (1:1 - 2:1 - 3:1) كما يلي:

- النموذج الأول: 12x36m بنسبة طول: عرض = 1:3
- النموذج الثاني: 12x24m بنسبة طول: عرض = 2:1
- النموذج الثالث: 12x12m بنسبة طول: عرض = 1:1

النمادج المستخدمة ذات عناصر أفقية (الكمرات) ببعض ثابتة = 50x25 سم بينما مقاسات العناصر الرأسية (العمودية) تبدأ ب 70x70 سم في البلاط الأول مع وضع في الاعتبار تقليص أبعاد العمود بعدد 5 سم كل دورين من الاتجاهين. لاقل مقاس للعمود = 40 سم والبلاطات التي تم عمل دراسة مقاومة عليها في النماذج المختلفة بسماك 8 سم - 10 سم - 12 سم كما تمت الدراسة أيضاً بغرض عدم وجود البلاطات. هذه الدراسة على كمال منظمة الدور.

تمت الدراسة اللاتخطية للمباني باستخدام سجل زمني لزلزال Elcentro بعجلة زلزالية قصوى مقدارها 0.5g وتتم التحليل باستخدام برامج التحليل الإنشائي ساب2000 ودراسة تأثير النماذج على البلاطات أثناء الارتفاع عالية الارتفاع تم عمل مقاومة لرود الأفعال الناتجة لكل نموذج مع تغيير سمة البلاطة ورود الأفعال التي تم دراستها هي:

- الإحرازات الأفقية على مستوى كل دور (U1)
- قوى الفص القاعدي لمنشأة كل ككل.

حيث تم تعيين الإحرازات لكل دور في النماذج للفصلتين نقطة (1) على طرف النموذج و نقطة (2) في منتصف البلاطة بعد إجراء التحليل الإنشائي للمباني المختلفة يمكن تلخيص النتائج الآتية:

Lateral displacements

1. لوحظ أنه زيادة سمك البلاطة تزيد جسمتها مما يعكس على زيادة جسمة المبنى ككل فيقل متوسط إحرازات المبنى ككل.
M. N. Mohamed et al., Effect of slabs in space framed structures under seismic loading, pp. 2065 - 2078
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2. As an increase in slab thickness results in a decrease in the frequency of structural failures (1) and (2), the damage is lower when the slabs are 12 mm thick.

3. It is observed that an increase in slab thickness leads to an increase in the frequency of structural failures. The highest damage occurred when the slabs were 12 mm thick. The damage in the first case was 12%.

4. Chipping of brick and mortar in the slab occurred at a ratio of 1:1, 1:2, and 1:3, respectively.

Base Shear

- 4. The force on the slab is determined by the mass of the slab and the acceleration of gravity.

From the above, it is clear that the damage caused by the slab is higher when the slab thickness is increased, which is consistent with the following equation.

The equation is:

\[ \text{Base Shear} = \frac{\text{Mass of Slab} \times \text{Acceleration of Gravity}}{\text{Slab Thickness}} \]

5. It is concluded that the slab should be designed to have a thickness of at least 12 mm to ensure structural integrity and stability.

6. It is recommended that further research be conducted to determine the optimal thickness of slabs for different types of structures.