ANALYSIS OF CHANNEL CODING PERFORMANCE FOR IMAGE TRANSMISSION OVER COOPERATIVE RELAY NETWORKS

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ABSTRACT:
In this paper, we examine and investigate the effects of noise-induced transmission errors on the performance of image transmission over cooperative relay networks with various error-correction capabilities. First, the relationships between lengths of the code, peak signal-to-noise ratio, and signal-to-noise ratio are analyzed. Second, the comparison between the performances of different channel coding is introduced in conjunction with the set partitioning in hierarchical trees algorithm as a source code. Genetic algorithm, as an efficient optimization technique, is applied for solving the problem of optimal unequal error protection method to reduce the transmission rate and to improve the transmitted image quality. Many useful and significant results that are introduced in this paper can be used in the enhancement of image transmission over the cooperative networks. Compared to traditional methods, the suggested method is more practical for the transmission of images with high-quality via smart devices.
Keywords: Image transmission; BCH coding; Cooperative Relay network; MAP.

1. Introduction

With the evolution of multimedia communications and the rapid outgrowth of the Internet, images have become the most common data exchanged [1]. The transmission links normally are subject to different sources of fading effects and noise with the limited bandwidth of the transmission channels [2]. Therefore, the necessity of image protection, image compression, and fault tolerance is a critical issue in reducing the required transmission bandwidth and transmission time.

Several techniques have been suggested to minimize the bit rate and induced errors with achieving higher received image quality [3]. However, it is difficult to decode and reconstruct the image under fault conditions while maintaining acceptable quality. Error Correction Codes (ECC) [4-6] help in detecting and correcting errors in the transmitted data. ECC diagrams have a limit on the maximum number of errors that can be addressed or corrected. The Set partitioning in hierarchical trees (SPIHT) algorithm [7] is an image coding algorithm that is modified in [8] to transmit images through various channels with the strong transmission. The error protection system leans towards the important data in the transmitted image and video which is the case in most unequal protection techniques (UEP) [8-9]. An extensive review of the large variation of error protection schemes is introduced in [10-11]. For an efficient error detecting and correcting code, the Bose–Chaudhuri–Hocquenghem (BCH) code was used in [12] because of its strong ability to randomize and detonate correction. An adaptive BCH scheme was proposed in [12] to choose the correction capabilities that offer the reconstructed image at high quality at a given SNR.

Recently, cooperative relay [13] is rapidly gaining interest in this multi-intermediary device (relays) that can cooperate to improve the overall relays network performance. They benefit from the nature of transmission provided by the wireless medium, whereby the transmitted signals can be received and processed by any device in the coverage area of the transmitter [13-15]. The main idea of network coding [16] is that information that comes from multiple sources is mixed (encoded), to boost the reliability of decoding at the destination. The literature has suggested many communication protocols [17], such as decoding and forwarding (DF), amplification and forwarding (AF), and compression and forward (CF). In this work, we consider the DF protocol as a communication protocol. The decoding scheme proposed in [16] presents the maximum a posterior decoder (MAP) for cooperative communication.
networks as the relay devices combine data received from sources to create the parity bits that are forwarded to the destination.

The Genetic algorithm (GA), as an advanced optimization technique, is derived from the notion of natural evolution based on the Darwinian theory of “survival of the fittest” by Holland [18]. In this paper, GA is utilized to get the optimum rate that minimizes the image distortion function. To conquer the specific disadvantages of static channel protection; there is a need for adaptive protection. Adaptive protection [20] adds redundancy data according to the channel behaviors and the importance of the different parts of the data. The authors in [21] introduced an adaptive scheme for image transmission over a cooperative network. They achieved both energy efficiency and image quality under the complex wireless channel. The real-time transmission of images through a multimode fiber (MMF) is still a challenging research work. One method completes image transmission by measuring and controlling the full complex field of the MMF [22]. To improve the image data transmission efficiency in the satellite communication systems, a class of rateless codes which can provide unequal error protection (UEP) property and equal waterfall region performance is proposed in this paper [23]. This paper analyzes the effects of noise on image transmission through the cooperative relay network when the channel coding is used. First, the relationships between bit error rate, signal-to-noise ratio (SNR), and code lengths are analyzed. Moreover, the transmission performance of BCH codes associated with different schemes is analyzed. This paper is arranged as follows. The problem formulation is introduced in Section 2. The proposed scheme is presented in Section 3. Numerical results and discussions are mentioned in Section 4. Conclusions are mentioned in Section 5.

2. Problem Formulation

In this section, the problem of FEC using channel coding will be presented. Assume the image is encoded by the modified SPIHT coder [8]. The generated bit stream is divided into a series of packets. Let \( \Delta D_i > 0 \) indicates the expected reduction in distortion if the i-th packet is decoded correctly. The overall distortion can be written as follows [7]:

\[
D(L) = D_0 - \sum_{i=1}^{L} \prod_{v=1}^{i} \varphi_v(r_v) \Delta D_i \quad (1)
\]

where \( D_0 \) is the expected distortion when the rate is zero, \( \varphi_v(r_v) \) is the probability that the v-th source packet is received correctly when it is sent by
a rate of \( r_v \). \( L \) is the number of the sent packets. Let \( P_v \) be the undetected error probability of the \( v \)-th packet. Then \( \varphi_v(r_v) \) can be written as follows:

\[
\varphi_v(r_v) = 1 - P_v
\]  

(2)

Then equation (1) can be rewritten as follows:

\[
D(L) = D_0 - \sum_{i=1}^{L} \prod_{v=1}^{i} (1 - P_v) \Delta D_i
\]  

(3)

The undetected error probability of the \( v \)-th packet bit \( P_v \) relies on the rate assigned to \( v \)-th packet \( r_v \) as shown in the next section. Therefore, the problem is to reduce the expected distortion \( D(L) \) according to the overall transmission rate limitations. We can formulate the problem as follows:

\[
\text{Min } D(L) \underbrace{\text{ subject to } \sum_{v=1}^{L} r_v \leq R}_{r}(4)
\]

where \( R \) is the total transmission rate.

### 2.1 Cooperative Relay Network

Without loss of generality, the cooperative network [16] shown in Fig. 1 is considered in this paper, that is consisting of two relays, two sources, and a destination. A transmission channel is assigned to each source. In the proposed work, the DF protocol is considered as the cooperation protocol. Firstly, the relays decode the data sent by the sources and then the relays combine them to create the parity bits. Data are sent using binary phase-shift keying (BPSK) modulation scheme. All channels are assumed to be Rayleigh fading channels with additive Gaussian noise (AWGN). The received signals at the destination at four consecutive channels are given by [16]

\[
y_i = g_i s_i \sqrt{d_i^{-z}} E_i + w_i \quad i = 1, 2, 3, 4
\]  

(5)

where

- \( y_i \) is the received signal from the \( i \)-th source for \( i = 1, 2 \) and from the \((i - 2)\)-th relay for \( i = 3, 4 \).
- \( g_i \) is the channel fading gain between the \( i \)-th source and the destination for \( i = 1, 2 \) and that between \((i - 2)\)-th relay and the destination for \( i = 3, 4 \).
- \( s_i \in \{+1, -1\} \), \( i = 1, 2 \), is the BPSK modulation of the \( i \)-th source bits, \( s_i \in \{+1, -1\} \), \( i = 3, 4 \) is the BPSK modulation of the \((i - 2)\)-th relay for \( i = 3, 4 \).
- \( d_i \) is the distance between the \( i \)-th source and the destination for \( i = 1, 2 \) and that between \((i - 2)\)-th relay and the destination for \( i = 3, 4 \).
• $E_i$ is the transmit energy of the $i$−th source for $i = 1, 2$ and $(i - 2)$−th relay for $i = 3, 4$.
• $z$ is the path loss exponent.
• $w_i$ is the white Gaussian noise with zero mean and variance $N_0/2$ between the $i$−th source and the destination for $i = 1, 2$ and that between $(i - 2)$−th relay and the destination for $i = 3, 4$.

The received signal can be written in a matrix form as follows [18]

$$Y = GS + W$$ (6)

where the received vector $Y = [y_1 \ y_2 \ y_3 \ y_4]^T$, the transmitted vector $S = [s_1 \ s_2 \ s_3 \ s_4]^T$, the noise vector $W = [w_1 \ w_2 \ w_3 \ w_4]^T$, and $G$ is given by

$$G = \begin{bmatrix}
g_1 \sqrt{d_1^{-z} E_1} & 0 & 0 & 0 \\
0 & g_2 \sqrt{d_2^{-z} E_2} & 0 & 0 \\
0 & 0 & g_3 \sqrt{d_3^{-z} E_3} & 0 \\
0 & 0 & 0 & g_4 \sqrt{d_4^{-z} E_4}
\end{bmatrix}$$ (7)

The MAP decoder [16] is used at the destination as it estimates the transmitted code word according to
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\[
P(c_i) = \frac{1}{(\pi N_0)^{\frac{3}{2}}} e^{-\frac{\|Y - GS_i\|^2}{2N_0}}
\]

\[
\hat{c} = \arg \max_w \frac{P(c_i)}{N_0}
\]

\[
= \arg \min_{c_i} \|Y - GS_i\|^2 - N_0 \log(P(c_i))
\]  

(8)

where \(P(c_i)\) is the transmitted probability of the codeword \(c_i\) that depends on the channel conditions between the sources and the relays. \(P_u\) is the upper bound for the probability of error that can be found in [16] and it is used later for optimizing the channel coding process.

2.2 Forward Error Correction with BCH Codes

In this paper, the BCH code [4] is used to correct errors escaped from the MAP decoder inside the cooperative network. BCH is an error-correcting code where a block code is defined by \((n, k)\), where \(n\) represents the size of the codeword and \(k\) represents the size of source bits, therefore, \((n - k)\) is the number of parity-check bits. A parameter \(t\) represents the maximum errors in the BCH codeword that can be corrected by the BCH code.

\[
n - k \leq mt
\]  

(9)

where \(n = 2^m - 1\), \(m\) is an integer positive number.

It is important to note that the larger the value \((n - k)\), the more error-correcting capability and the less size of the transmitted stream. However, the effectiveness of any error technique depends mainly on the channel conditions. Each source packet that has \(k\) bits is protected by \((n - k)\) parity bits producing a packet of size \(n\) using BCH code. Let the data are transmitted through the cooperative network described above with a bit error rate \(P_u\). Hence the undetected error probability of the \(v\) -th packet bits, \(P_v\) using BCH code can be estimated as follows [20]:

\[
P_v = 2^{-mt_v} \sum_{s=0}^{t_v} \binom{n}{s} \sum_{h=t_v+1}^{n} \binom{n}{h} P_u^h (1 - P_u)^{n-h}
\]  

(10)

where \(t_v\) represents the maximum the number of errors that can be corrected by the BCH code in the \(v\) -th block or packet. Substituting from (10) into (3) yields:

\[
D(L) = D_0 - \sum_{i=1}^{L} \prod_{p=1}^{i} (1 - 2^{-mt_v} \sum_{s=0}^{t_v} \binom{n}{s} \sum_{h=t_v+1}^{n} \binom{n}{h} P_u^h (1 - P_u)^{n-h} ) \Delta D_i
\]  

(11)
Hence, the expected distortion expression in (11) for the total transmission rate constraint can be minimized. The total redundancy bits can be estimated as follows:

\[ R_d = \sum_{i}^{L} mt_i = R - \text{(image data length from source coder)} \]  \hspace{1cm} (12)

Equation (12) represents the constraint that the optimization algorithm considers. Therefore, after the optimization process, the BCH coder can determine the needed redundancy \((n - k)\) to code every packet of the image data.

2.3 Genetic Algorithm (GA)

GA was inspired by the concept of natural evolution based on the Darwinian "survival of the fittest" theory by Holland [18]. The starting point for GA is the selection of the candidate solutions represented by the chromosomes, which in GA are like the population. A new population or a new generation was created by the old population. The choose of solutions or new offspring is suitable for their fitness. Hence, better solutions have greater production opportunities. The process is repeated until conditions are determined [19]. The advantages of GA over other common optimization techniques can be summarized [25] as follows:
a. GA can avoid trapping into local optima because Candidate solutions are better than normal techniques, as filter solutions have many points over normal techniques that have only one point.

b. GA is characterized by values and is not dependent on differentiation of other auxiliary elements.

c. GA is based on parameter set coding. Thus, the search process is applied to solve both integer and discrete problems.

d. Selection and crossover are used by GA to randomly select parents, so that exploration is performed to produce the best new offspring.

e. GA is used here to find the optimum rate $r_j$ of $j$-th image data packet that achieves the minimum overall distortion $D(L)$.

3. The Proposed Scheme

The block diagram of the proposed scheme is shown in Fig. 2. In the beginning, the image is encoded by the modified SPIHT coder [8]. The output from the modified SPIHT coder consists of four groups. Each group is different in its importance from each other. The importance of each packet in each group is analyzed in [8] then $\Delta D_i$ is estimated for each packet in the bit steam.

The proposed scheme can be summarized in the following points:

1) SPIHT image coding is modified to generate four groups of bit streams linked in order of importance, and then the output data is split into series of packets.

2) The reduction in distortion $\Delta D_i$ is approximately estimated.

3) Based on the number of the source packet, $\Delta D_i$ of each packet and the bit error probability of the cooperative network $P_u$, the optimization algorithm, that is GA, is used to generate the optimum value of $r_j$ of each packet subject to the total transmission rate constraint.

4) Based on the values of $r_j$ for $j = 1, \ldots, L$ determined by the optimization algorithm, the BCH encoder encodes each packet according to their significance.

5) The coded data is sent to the receiver through the relay network.

6) The MAP decoder at the receiver estimates the transmitted data.

7) The BCH decoder decodes the transmitted data, and it tries to correct the errors due to the transmission channel.

8) Finally, the image is reconstructed by the SPIHT decoder.
3. Numerical Results and Discussions

The proposed scheme is tested on a cooperative network with fading channels and AWGN channel. The mean of the square of fading gains are assumed to be unity. The tested image is a LENA image 512x512 grey scale. First, the original images are decomposed into sub-images using the wavelet transform with a 7-tap high-pass filter and a 9-tap low-pass filter [24]. In the proposed test, we only use 6 layers in the wavelet domain. Then the wavelet coefficients are converted to the source bit stream with a bit rate of 0.4 bpp using the modified SPIHT. The source bit stream is divided into four groups then each group is divided into packets. Initially, we tried to place the results of the unequal error protection (UEP) method in a comparison form with of the results of the equal error protection (EEP) method. Diversity is done through a network of one relay or two relays with different SNR and BER as will be shown in the simulation results. Fig. 3 shows an example of the channel rate allocation of UEP scheme produced by GA. More redundancy bits are assigned to the most significant data as shown in Fig. 3. Fig. 4 shows the average PSNR of the decoded LENA image against the transmission rate for equal error protection (EEP) and unequal error protection (UEP) coding method that transmitted through a one-relay cooperative network. The bit error rate for cooperative relay network $P_u$ is 0.0636 and the received SNR is 5dB. In the case of the EEP, all packets are protected by the same size of redundancy bits. In the case of UEP, each packet is protected by different redundancy bits according to its importance that is determined by the optimization algorithm. The total transmission rate is the same in the cases EEP and UEP. In the case of UEP, the GA optimization is used to determine the required channel coding rate $r_j$ for each packet which helps the BCH encoder to determine the parameters needed to work $(n,k)$. The results obtained by the UEP scheme outperform those obtained by the EEP scheme by 6 dB that reflects the high performance of the proposed scheme.
In the case of using two relays, Fig. 5 illustrates the average PSNR of the decoded LENA image as a function of the transmission rate for EEP and UEP coding method. The bit error rate for cooperative relay network $P_u$ is 0.03 and the received SNR is 5dB. Because the data is transmitted over two relays cooperative network that is reflected on the values of BER, the resulting PSNR of the decoding image is better than the obtained PSNR in one–relay cooperative network. Fig.6 shows the required transmission rate in three cases against the received SNR. The three cases are without any diversity, with aiding of one relay, and with aiding of two relays. With EEP channel coding (BCH), it is desired to achieve PSNR of 35dB in the three cases at different values of the received SNR. It is clear that the more using relays, the less required transmission rate.
Another interesting issue that has been investigated in this study is the effect of the length of the block of BCH code (n). Is there a value of BCH code block length having the best performance than others? Indeed, the answer to this question is yes. Fig. 7 shows the average PSNR performance for the two-relays network with a different block length n for BCH code at SNR=5db. Fig. 8 shows that at the same transmission rate and low BER, the resulting PSNR differs for the three cases of a different block length. It is found that the resulting PSNR is higher at a block length of 1023 than that PSNR at block length of 2047 and PSNR at a block length of 16383. The interpretation of this issue is very easy. If the number of transmitted block errors exceeded t errors, the BCH decoder will not be able to correct the error in the transmitted block despite the block length. The errors occur randomly during transmission. Due to the fading channel nature, the errors are not uniformly distributed between
data packets. So, the error may be larger in a block than others so the BER $P_u$ may be very different than $\left(\frac{t}{n}\right)$. Because the error in a small block length is significant than the error in a large block length, we may get a high PSNR with using a small block length. For example, if four packets are sent with block length $n = 1023$, assuming packet 1,2,3,4 has an error of 5,15,10,25 bits during the transmission process respectively, and $(t) = 15$, packet 1, 2, 3 will be received correctly and packet 4 will be received with error. Now, if we decide to send the same data using two packets only of length $n = 2047$, and if the packets 1, 2 has an error of 20, 35 bits respectively, and $(t) = 30$ then packet "1" will be received correctly and packet "2" is received with error. Notice packet "2" in the second case includes the data of packet 3, 4 of the first case which means that data of packet 3 is received correctly when $n = 1023$ and it is received with error when $n = 2047$. This explains why the block length is very important in the BCH coding process. Fig. 8 confirms the same idea as shown in Fig. 7.

![Fig. 7](image)

**Fig. 7** The PSNR of a two-relay network at different codeword lengths of BCH code at 5dB SNR.

However, in Fig. 8, the best value of $(n)$ is 8191 because SNR =10dB so the network has better BER performance than in Fig. 6. It is shown that the best value of block length $(n)$ relies on the BER value of the cooperative network $(P_u)$. i.e., the larger value of BER $(P_u)$, the smaller value of the best BCH block length $(n)$.
Another interesting issue that has been investigated in this study is the comparison between the BCH code and the rate-compatible punctured convolutional code (RCPC) code [4]. Fig. 9 shows the transmission rate in bpp performance using a one-relay network with BCH and RCPC channel coding at SNR=5, 10, 15, 20 and the output PSNR is 35dB for different values of SNR. It is shown that, in the case of a high BER and a low SNR, the RCPC code performance is better than the performance of the BCH code because it requires less transmission rate than the BCH code to achieve PSNR=35db. With decreasing BER value and increasing SNR values, BCH code performance is better than RCPC performance because it requires a low transmission rate compared to RCPC code. Fig. 10 shows the transmission rate in bpp performance using a two-relay network with BCH and RCPC channel coding at SNR=5, 10, 15, 20 at output PSNR of 35dB for different values of SNR.

The BCH code performance outperforms the RCPC performance with improving in the BER performance. Fig.11 and Fig.12 show the average PSNR performance for two-relay and three relays network respectively, under BCH and RCPC channel coding with the transmission rate in bpp. It is shown that PSNR in case of using BCH is larger than in in case of using RCPC.
Fig. 9 Comparison between BCH and RCPC performance of one-relay network.

Fig. 10 Comparison between BCH and RCPC performance of two-relay network.

Fig. 11 The PSNR of a two-relay network for BCH and RCPC at 5dB SNR.
Another interesting issue that has been investigated in this study is the comparison between the BCH code and the low-density parity check matrix (LDPC) code [25]. Fig. 13 shows the transmission rate in bpp performance using a one-relay network with BCH and LDPC channel coding at SNR=3, 5, 7, 10, 15, 20 at PSNR of 35dB for different values of SNR. It is shown that, in the case of a high BER and a low SNR, the LDPC code performance is better than the performance of the BCH code because it requires less transmission rate than the BCH code to achieve PSNR=35db. With decreasing BER value and increasing SNR values, BCH code performance is better than LDPC performance because it requires a low transmission rate compared to the LDPC code.

**Fig. 12** The PSNR of a three-relay network for BCH and RCPC at 5dB SNR.

**Fig. 13** Comparison between BCH and LDPC performance of two-relay network.
6. Conclusions

In this work, the study and analysis of three channel coding for image transmission over cooperative networks are introduced. The system used for the analysis is proposed for the transmission of image streams over the fading channel through a cooperative relay network. Genetic algorithm is considered as an optimization technique is applied for finding the optimum channel allocation rates of the coding in all packets. The inputs to the optimization algorithm are the number of source packets, the bit error rate (BER), and the model of the distortion function. The BCH code is used to protect the image by adding redundancy bits according to the number of errors that can be corrected according to the used optimization technique. The optimum packet size is used with different BER with two relays. RCPC code performance is investigated in the case of using two relays, one relay, and without using any relays, and its performance is compared with BCH code performance with image PSNR and transmission rate. The simulation results show that BCH code performance is better than RCPC and LDPC performance in the case of a high received signal to noise ratio. However, the RCPC and LDPC performance is better than the BCH performance at high BER. The research work is done using MATLAB, other Special Network Simulation Tools/SW Packages will be considered for future work.

References


